

Exam 3 – Multi-Particle Systems

November 20, 2012

This is a closed book examination. You may use a both sides of a 3"x5" notecard (or one side of a 4"x6" notecard) with equations, concepts or other soothing sonnets. There is extra scratch paper available. Your explanation is worth $\frac{3}{4}$ of the points. Explain your answers!

A general reminder about problem solving:

1. Draw a picture then create a simplified free body diagram with all forces
 2. Write down what you know including coordinate frame
 3. Write down what you don't know and/or want to know
 4. List mathematical relationships
 5. Simplify and solve
 6. Check your answer – Is it reasonable? Are units correct?
 - Show all work!
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1. [4 PTS] The first excited state of a particular atom in a gas is 7.3 eV above the ground state. A moving electron collides with one of these atoms, and excites the atom to its first excited state. Immediately after the collision the kinetic energy of the electron is 3.1 eV. What was the kinetic energy of the electron just before the collision?
 - a) 4.2 eV
 - b) 5.2 eV
 - c) 6.6 eV
 - d) 7.9 eV
 - e) 10.4 eV

 2. [4 PTS] What is the rotational kinetic energy of an object rotating at 50 rad/s with a moment of inertia of 30 kg m²?
 - a) 41.7 J
 - b) 1.50×10^3 J
 - c) 2.25×10^4 J
 - d) 3.75×10^4 J
 - e) 7.50×10^4 J

 3. [6 PTS] An elastic collision is different from an inelastic collision. Indicate which of the following statements about an elastic collision are **True** and which are **False**. Explain
 - a) ___ The sum of the final kinetic energies equals the sum of the initial kinetic energies.
 - b) ___ The colliding objects are stretchy or squishy.
 - c) ___ The colliding objects stick together.
 - d) ___ The momentum is only conserved in an elastic collision.
 - e) ___ There is no change in the internal energies of the objects (thermal energy, vibrational energy, etc.).

The next two questions concern the collision between an 8 kg mass initially traveling at $\langle 12, 0, 0 \rangle$ m/s and a 12 kg mass initially travelling at $\langle 4, 0, 0 \rangle$ m/s. The two masses stick together after the collision.

4. [4 PTS] What is the final velocity?
 - a) $\langle 2.4, 0, 0 \rangle$ m/s
 - b) $\langle 3.0, 0, 0 \rangle$ m/s
 - c) $\langle 7.2, 0, 0 \rangle$ m/s
 - d) $\langle 48, 0, 0 \rangle$ m/s
 - e) $\langle 144, 0, 0 \rangle$ m/s

5. [4 PTS] What is the increase in internal energy of the two masses?
 - a) 154 J
 - b) 518 J
 - c) 614 J
 - d) 672 J
 - e) 1190 J

6. [4 PTS] A solid sphere and a solid disk are both spinning at the same angular velocity. If they both have the same radius which object has more rotational kinetic energy?
 - a) The solid sphere has more rotational kinetic energy
 - b) The solid disk has more rotational kinetic energy
 - c) They both have the same rotational kinetic energy
 - d) Not enough information given to determine which has greater rotational kinetic energy.

The next two questions concern two identical solid disks are placed at the same height on a hill to race. The red disk is placed on a track with a non-slip pad so it will roll without slipping. The green disk is placed on a “frictionless” pad so it will slide down the hill without rolling.

7. [4 PTS]. Which disk is traveling faster?
 - a) The red disk is traveling faster.
 - b) The green disk is traveling faster.
 - c) Both disks are traveling the same speed.
 - d) Not enough information.

8. [4 PTS] Which disk has more total energy at the bottom of the hill?
 - a) The red disk has more energy.
 - b) The green disk has more energy.
 - c) Both disks have the same energy.
 - d) Not enough information.

9. [6 PTS] An “atom” has energy levels of -15.2 eV, -5.3 eV and -3.6 eV. A collection of these atoms is bombarded by an electron beam so that there are atoms with electrons in every excited state. Indicate which of the following energy photons will be observed (True) and which will not be seen (False). Explain.
- a) ___ 1.7 eV
 - b) ___ 8.9 eV
 - c) ___ 9.9 eV
 - d) ___ 11.6 eV
 - e) ___ 18.8 eV
 - f) ___ 20.5 eV
 - g) ___ No photons observed since energies are negative.

Please do the next two problems using problem solving sheets (or on additional paper).

10. [12 PTS] A square made with four 2.0 meter long nanotubes has small dense 3 kg objects placed at each corner. The nanotubes are really strong and basically massless. You want to store the maximum energy when spinning this object at a fixed angular frequency. Calculate the difference in energy for spinning it about a diagonal or about an edge.
11. [12 PTS] An object with a mass of 0.15 kg hits the floor with a speed of 5 m/s after falling 59 meters. The object rebounds upward from the floor with a speed of 4.2 m/s after being in contact with the floor for 0.0016 sec. Compare the average force exerted by the floor to the gravitational force on the object.

Possibly useful mathematical relationships:

$\sin^2(\theta) + \cos^2(\theta) = 1$	$\sin(2\theta) = 2 \sin(\theta) \cos(\theta)$
$\cos(2\theta) = \cos^2(\theta) - \sin^2(\theta) = 2 \cos^2(\theta) - 1 = 1 - 2 \sin^2(\theta)$	
Derivative of a polynomial $\frac{d}{du} Cu^n = nCu^{n-1}$	
Anti-derivative (integral) of a polynomial $\int Cu^n du = \frac{1}{n+1} Cu^{n+1} + const.$	
The Chain Rule $\frac{d}{dz} f(u) = \frac{d}{dz} u \frac{d}{du} f(u)$	

Useful Data:

Mass of Earth = 6×10^{24} kg	$G = 6.67 \times 10^{-11} \text{ Nm}^2/\text{kg}^2$
Radius of the Earth = 6.4×10^6 m	Acceleration due to gravity at the surface of the earth is 9.81 m/s^2